## THINK AND DISCUSS

1. How do you know that a direct variation is linear?
2. Why does the graph of any direct variation pass through $(0,0)$ ?
3. GET ORGANIZED Copy and complete the graphic organizer. In each box, describe how you can use the given information to identify a direct variation.

| Recogni ing a Direct Variation |  |  |
| :---: | :---: | :---: |
| From an Equation | From Ordered Pairs | From a Graph |



## GUIDED PRACTICE

1. Vocabulary If $x$ varies directly with $y$, then the relationship between the two variables is said to be a $\qquad$ ? . (direct variation or constant of variation)

SEE EXAMPLE 1
p. 326

Tell whether each equation represents a direct variation. If so, identify the constant of variation.
2. $y=4 x+9$
3. $2 y=-8 x$
4. $x+y=0$

SEE EXAMPLE 2 Tell whether each relationship is a direct variation. Explain.
p. 327
5.

| $x$ | 10 | 5 | 2 |
| :---: | :---: | :---: | :---: |
| $y$ | 12 | 7 | 4 |

6. 

| $x$ | 3 | -1 | -4 |
| :---: | ---: | ---: | ---: |
| $y$ | -6 | 2 | 8 |

7. The value of $y$ varies directly with $x$, and $y=-3$ when $x=1$. Find $y$ when $x=-6$.
8. The value of $y$ varies directly with $x$, and $y=6$ when $x=18$. Find $y$ when $x=12$.

SEE EXAMPLE 4
p. 328
9. Wages Cameron earns $\$ 5$ per hour at her after-school job. The total amount of her paycheck varies directly with the amount of time she works. Write a direct variation equation for the amount of money $y$ that she earns for working $x$ hours. Then graph.

## PRACTICE AND PROBLEM SOLVING

Tell whether each equation represents a direct variation. If so, identify the constant of variation.
10. $y=\frac{1}{6} x$
11. $4 y=x$
12. $x=2 y-12$

Tell whether each relationship is a direct variation. Explain.
13.

| $x$ | 6 | 9 | 17 |
| :---: | :---: | :---: | :---: |
| $y$ | 13.2 | 19.8 | 37.4 |

14. 

| $x$ | -6 | 3 | 12 |
| :---: | ---: | ---: | ---: |
| $y$ | 4 | -2 | -8 |


| Independent Practice <br> For <br> Exercises | See <br> Example |
| :---: | :---: |
| $10-12$ | 1 |
| $13-14$ | 2 |
| $15-16$ | 3 |
| 17 | 4 |

## Extra Practice

Skills Practice p. S13
Application Practice p. S32


Astronomy


The Mars rover Spirit landed on Mars in January 2004 and immediately began sending photos of the planet's surface back to Earth.
15. The value of $y$ varies directly with $x$, and $y=8$ when $x=-32$. Find $y$ when $x=64$.
16. The value of $y$ varies directly with $x$, and $y=\frac{1}{2}$ when $x=3$. Find $y$ when $x=1$.
17. While on his way to school, Norman saw that the cost of gasoline was $\$ 2.50$ per gallon. Write a direct variation equation to describe the cost $y$ of $x$ gallons of gas. Then graph.

Tell whether each relationship is a direct variation. Explain your answer.
18. The equation $-15 x+4 y=0$ relates the length of a videotape in inches $x$ to its approximate playing time in seconds $y$.
19. The equation $y-2.00 x=2.50$ relates the cost $y$ of a taxicab ride to distance $x$ of the cab ride in miles.

Each ordered pair is a solution of a direct variation. Write the equation of direct variation. Then graph your equation and show that the slope of the line is equal to the constant of variation.
20. $(2,10)$
21. $(-3,9)$
22. $(8,2)$
23. (1.5, 6)
24. $(7,21)$
25. $(1,2)$
26. $(2,-16)$
27. $\left(\frac{1}{7}, 1\right)$
28. $(-2,9)$
29. $(9,-2)$
30. $(4,6)$
31. $(3,4)$
32. $(5,1)$
33. $(1,-6)$
34. $\left(-1, \frac{1}{2}\right)$
35. $(7,2)$

Astronomy Weight varies directly with gravity. A Mars lander weighed 767 pounds on Earth but only 291 pounds on Mars. Its accompanying Mars rover weighed 155 pounds on Mars. How much did it weigh on Earth? Round your answer to the nearest pound.
37. Environment Mischa bought an energy-efficient washing machine. She will save about 15 gallons of water per wash load.
a. Write an equation of direct variation to describe how many gallons of water $y$ Mischa saves for $x$ loads of laundry she washes.
b. Graph your direct variation from part a. Is every point on the graph a solution in this situation? Why or why not?
c. If Mischa does 2 loads of laundry per week, how many gallons of water will she have saved at the end of a year?
38. Critical Thinking If you double an $x$-value in a direct variation, will the corresponding $y$-value double? Explain.
39. Write About It In a direct variation $y=k x, k$ is sometimes called the "constant of proportionality." How are proportions related to direct variations?


