## THINK AND DISCUSS

1. Use the FOIL method to verify that $(a+b)(a-b)=a^{2}-b^{2}$.
2. When a binomial is squared, the middle term of the resulting trinomial is twice the $\qquad$ of the first and last terms.

3. GET ORGANIZED Copy and complete the graphic organizer. Complete the special product rules and give an example of each.

| Special Products of Binomials |  |  |
| :---: | :---: | :---: |
| $\begin{array}{c}\text { Perfect-Square } \\ \text { Trinomials }\end{array}$ |  |  | \(\left.\begin{array}{c}Difference of <br>

Two Squares\end{array}\right]\)

## GUIDED PRACTICE

1. Vocabulary In your own words, describe a perfect-square trinomial.

## SEE EXAMPLE 1 <br> p. 501

## Multiply.

| SEE EXAMPLE |  |
| ---: | ---: |
| p. 502 | $\mathbf{2}$ |
| SEE EXAMPLE | $\mathbf{3}$ |
| p. 503 | $\square$ |

2. $(x+7)^{2}$
3. $(2+x)^{2}$
4. $(x+1)^{2}$
5. $(2 x+6)^{2}$
6. $(5 x+9)^{2}$
7. $(2 a+7 b)^{2}$
8. $(x-6)^{2}$
9. $(x-2)^{2}$
10. $(2 x-1)^{2}$
11. $(8-x)^{2}$
12. $(6 p-q)^{2}$
13. $(7 a-2 b)^{2}$
14. $(x+5)(x-5)$
15. $(x+6)(x-6)$
16. $(5 x+1)(5 x-1)$
17. $\left(2 x^{2}+3\right)\left(2 x^{2}-3\right)$
18. $\left(9-x^{3}\right)\left(9+x^{3}\right)$
19. $(2 x-5 y)(2 x+5 y)$

SEE EXAMPLE 4 p. 503
20. Geometry Write a polynomial that represents the area of the figure.


## PRACTICE AND PROBLEM SOLVING

| Independent Practice <br> For <br> Exercises | See <br> Example |
| :---: | :---: |
| $21-26$ | 1 |
| $27-32$ | 2 |
| $33-38$ | 3 |
| 39 | 4 |

Extra Practice
Skills Practice p. S17
Application Practice p. S34

Multiply.
21. $(x+3)^{2}$
22. $(4+z)^{2}$
23. $\left(x^{2}+y^{2}\right)^{2}$
24. $\left(p+2 q^{3}\right)^{2}$
25. $(2+3 x)^{2}$
26. $\left(r^{2}+5 t\right)^{2}$
27. $\left(s^{2}-7\right)^{2}$
28. $\left(2 c-d^{3}\right)^{2}$
29. $(a-8)^{2}$
30. $(5-w)^{2}$
31. $(3 x-4)^{2}$
32. $\left(1-x^{2}\right)^{2}$
33. $(a-10)(a+10)$
34. $(y+4)(y-4)$
35. $(7 x+3)(7 x-3)$
36. $\left(x^{2}-2\right)\left(x^{2}+2\right)$
37. $\left(5 a^{2}+9\right)\left(5 a^{2}-9\right)$
38. $\left(x^{3}+y^{2}\right)\left(x^{3}-y^{2}\right)$
39. Entertainment Write a polynomial that represents the area of the circular puzzle. Remember that the formula for area of a circle is $A=\pi r^{2}$, where $r$ is the radius of the circle. Leave the symbol $\pi$ in your answer.
40. Multi-Step A square has sides that are $(x-1)$ units long and a rectangle has a length of $x$ units and a width of $(x-2)$ units.
a. What are the possible values of $x$ ? Explain.
b. Which has the greater area, the square or the rectangle?
c. What is the difference in the areas?


Multiply.
41. $(x+y)^{2}$
42. $(x-y)^{2}$
43. $\left(x^{2}+4\right)\left(x^{2}-4\right)$
44. $\left(x^{2}+4\right)^{2}$
45. $\left(x^{2}-4\right)^{2}$
46. $(1-x)^{2}$
47. $(1+x)^{2}$
48. $(1-x)(1+x)$
49. $\left(x^{3}-a^{3}\right)\left(x^{3}-a^{3}\right)$
50. $(5+n)(5+n)$
51. $(6 a-5 b)(6 a+5 b)$
52. $\left(r-4 t^{4}\right)\left(r-4 t^{4}\right)$

Copy and complete the tables to verify the special products of binomials.


Beginning about 3000 B.c.e., the Babylonians lived in what is now Iraq and Turkey. Around 575 b.c.e., they built the Ishtar Gate to serve as one of eight main entrances into the city of Babylon. The image above is a relief sculpture from a restoration of the Ishtar Gate.

| $a$ | $b$ | $(a-b)^{2}$ | $a^{2}-2 a b+b^{2}$ |
| :---: | :---: | :---: | :---: |
| 1 | 4 | $(1-4)^{2}=9$ | $1^{2}-2(1)(4)+4^{2}=9$ |
| 2 | 4 |  |  |
| 3 | 2 |  |  |

55. 

| $a$ | $b$ | $(a+b)^{2}$ | $a^{2}+2 a b+b^{2}$ |
| :---: | :---: | :---: | :---: |
| 1 | 4 |  |  |
| 2 | 5 |  |  |
| 3 | 0 |  |  |

57. 

| $a$ | $b$ | $(a+b)(a-b)$ | $a^{2}-b^{2}$ |
| :---: | :---: | :---: | :---: |
| 1 | 4 |  |  |
| 2 | 3 |  |  |
| 3 | 2 |  |  |

61. Math History The Babylonians used tables of squares and the formula $a b=\frac{(a+b)^{2}-(a-b)^{2}}{4}$ to multiply two numbers. Use this formula to find the product $35 \cdot 24$.
62. Critical Thinking Find a value of $c$ that makes $16 x^{2}-24 x+c$ a perfect-square trinomial.
63. ///ERROR ANALYSIS/// Explain the error below. What is the correct product? $(a-b)^{2}=a^{2}-b^{2}$
